

# Leakage Bounds for Gaussian Side Channels

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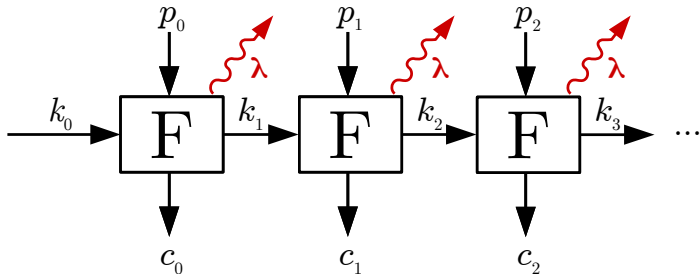
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# Content

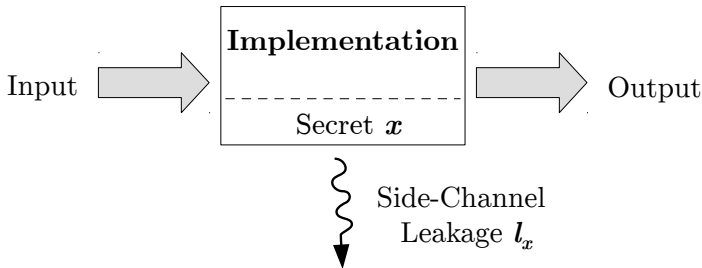
- Side-channel attacks threaten embedded devices
- Leakage-resilient schemes offer bounded leakage
- Challenge: specify leakage of underlying primitive
- This work: new approach to quantify leakage under a single data input
  - Mutual information in multivariate leakages: capacity of  $n$ -to- $m$  communication channels
  - Channel capacity: (multivariate) SNR in  $m$  POIs
  - Averaging  $N$  traces: SNR increases  $\sim N^m$
  - Practical verification: KECCAK- $f$ [400] on ASIC

# Motivation



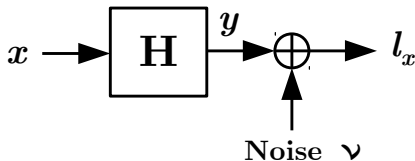
- Key update inherently prevents DPA
- Total leakage is bounded given  $\lambda$ -bit leakage of  $F$
- Practical question: what is the value of  $\lambda$ ?

# Leakage Quantification



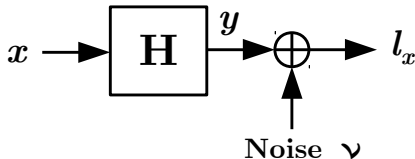
- Attacker tries to learn  $x$  from  $l_x$
- Quantify information about  $x$  in  $l_x$ 
  - Mutual information
  - $MI(X, L_x) = H[X] - H[X|L_x]$

# Channel Model



- Channel  $H$ : leakage behavior of implementation
- Linear  $m \times n$  channel matrix  $H$ :
  - $l_x = Hx + \nu$
- Secret state  $x$ :  $n \times 1$  vector (for  $n$ -bit state)
- Leakage trace  $l_x$ :  $m \times 1$  vector (for  $m$  POIs)
- Noise  $\nu$ :  $m \times 1$  vector

# Channel Capacity



- Maximize mutual information between  $x$  and  $l_x$ 
  - Channel capacity  $C = \max_{p(X)} MI(X, L_x)$
- Similar to Multi-Input Multi-Output (MIMO) channels
  - Wireless communication:  $n$  senders,  $m$  receivers

# Capacity of MIMO Channels

- Capacity of MIMO channel (fixed  $\mathbf{H}$ ):

$$C = \max_{\Sigma_{\mathbf{x}}: \text{tr}(\Sigma_{\mathbf{x}}) = P} \log_2 |\mathbf{I}_m + \mathbf{H}\Sigma_{\mathbf{x}}\mathbf{H}^H|$$

- $n \times n$  signal covariance matrix  $\Sigma_{\mathbf{x}}$
- Gaussian white noise with  $\sigma_{\nu}^2 = 1$
- Side channels:
  - No power constraint  $P$
  - Real values, e.g., power, no complex numbers
  - Noise correlations and different variances

# Capacity of Gaussian Side Channels (1)

- Capacity of Gaussian Side Channels

$$C = \max_{p(X)} MI(X, L_x) = \frac{1}{2} \log_2 |\mathbf{I}_m + \Sigma_\nu^{-1} \mathbf{H} \Sigma_x \mathbf{H}^H|.$$

- $m \times m$  noise covariance matrix  $\Sigma_\nu$



## Capacity of Gaussian Side Channels (2)

$$C = \frac{1}{2} \log_2 |\mathbf{I}_m + \Sigma_\nu^{-1} \mathbf{H} \Sigma_{\mathbf{x}} \mathbf{H}^H|$$

- Channel matrix  $\mathbf{H}$  is typically unknown...
- Profile side channel: multivar. Gaussian distribution
  - Templates:  $(\mu_i, \Sigma_{\nu,i})$  for all possible states  $\mathbf{x}_i$
- Independent noise: estimate  $\Sigma_\nu$  from  $\Sigma_{\nu,i}$
- Means  $\mu_i$  give  $\Sigma_{\mathbf{y}}$  (corresponding to  $\mathbf{y} = \mathbf{H}\mathbf{x}$ )
  - $\Sigma_{\mathbf{y}} = \mathbf{H} \Sigma_{\mathbf{x}} \mathbf{H}^H$

# Leakage from Gaussian Side Channels

- Channel capacity:  $C = \frac{1}{2} \log_2 |\mathbf{I}_m + \Sigma_\nu^{-1} \Sigma_y|$
- Multivariate SNR:  $\Sigma_\nu^{-1} \Sigma_y$ 
  - Reflects correlations in signal and noise
  - Device- and measurement-specific
- Univariate leakage:
  - $C = \frac{1}{2} \log_2 \left( 1 + \frac{\sigma_y^2}{\sigma_\nu^2} \right) = \frac{1}{2} \log_2 (1 + SNR)$

# Averaging Attacker

# Averaging Attacker

- Attackers observe the same operation multiple times
  - E.g., decryption of an FPGA bitfile
- Average  $N$  leakage traces  $I_x$  to remove noise
  - Noise covariance changes:  $\bar{\Sigma}_\nu = \frac{1}{N} \Sigma_\nu$
  - Channel capacity increases:

$$C = \frac{1}{2} \log_2 \left| \mathbf{I}_m + N \cdot \Sigma_\nu^{-1} \Sigma_y \right|$$

# Estimated Attack Complexity

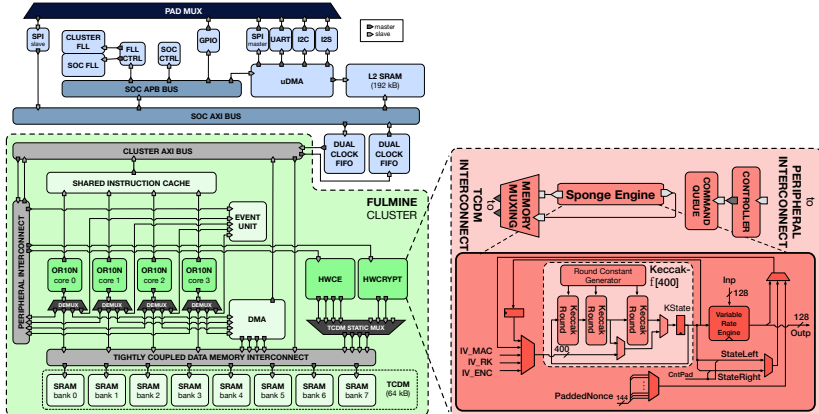
- Averaging a large number of traces
  - $C \approx \frac{1}{2} \log_2 (1 + N^m |\Sigma_{\nu}^{-1} \Sigma_{\mathbf{y}}|)$
- Scalar, single-trace  $SNR_m = |\Sigma_{\nu}^{-1} \Sigma_{\mathbf{y}}|$
- Leakage proportional to  $N^m$
- Number of averaged traces  $N$  reflects attack complexity
  - Tool for both attackers and designers

# Experimental Evaluations

# Experimental Evaluations

- Implementation of KECCAK- $f$ [400]-based ISAP
  - Leakage-resilient authenticated encryption
  - Specifies leakage bounds for 128-bit security
- Two kind of evaluations:
  - Verify soundness of leakage bounds
    - Evaluate MI and channel capacity on hardware
  - Estimate security of ISAP implementation

# Evaluation Hardware: FULMINE

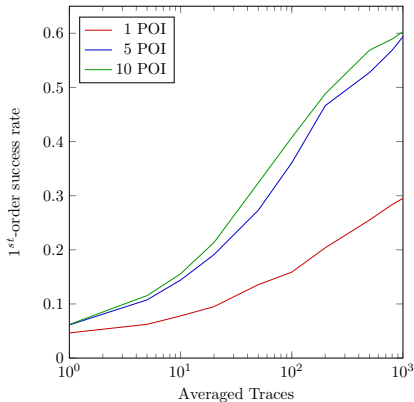
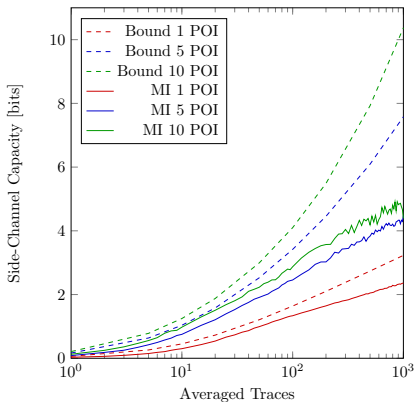




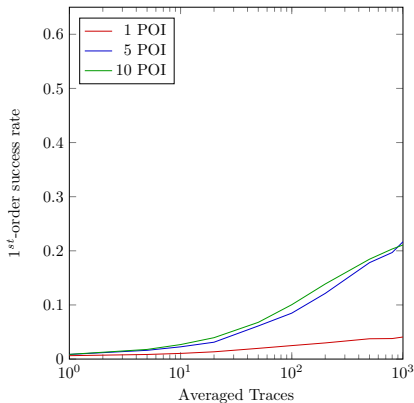
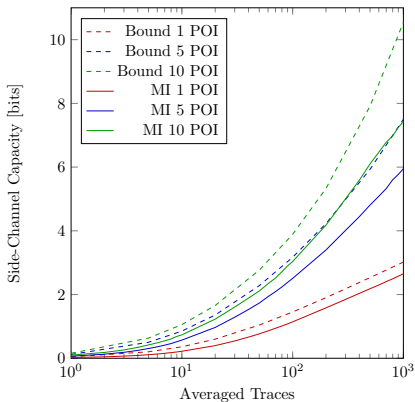
# Methodology

- Creation of multivariate Gaussian power templates
  - 5- and 8-bit parts of 400-bit KECCAK- $f$ [400] state
  - Remaining state held constant
- Training phase: 1400 measurements per class
- Choice of POIs:
  - Points of highest variance
  - Maintain a certain minimum distance
  - Register and combinatorial activity

# Capacity and Mutual Information (32 classes)



# Capacity and Mutual Information (256 classes)

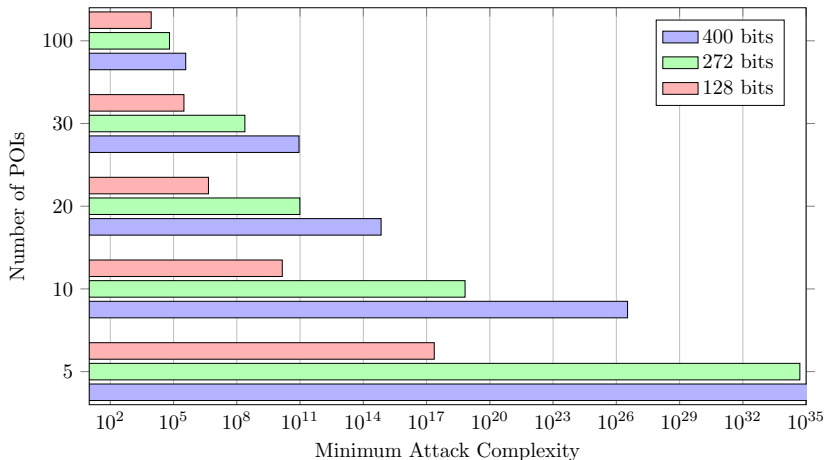


# Security Estimation of ISAP

- Large state size
  - 400-bit KECCAK- $f$ [400] state
  - Template building infeasible
- $SNR_m = |\Sigma_\nu^{-1}\Sigma_y|$  is relevant for leakage quantification
  - $SNR_m$  determined for 5- and 8-bit templates
  - Estimation for larger state: security margin  $\gamma$

$$N = \left( \frac{2^{2S} - 1}{\gamma \cdot SNR_m} \right)^{1/m}$$

# Security of ISAP on FULMINE ( $\gamma = 100$ )



# Conclusion

- Leakage quantification is of ongoing interest
- Method to quantify the leakage from Gaussian side channels
  - Capacity of  $n$ -to- $m$  communication channels
- Leakage bounded by physical property: SNR
- Averaging  $N$  traces: SNR increases  $\sim N^m$ 
  - Tool to estimate the attack complexity
- Practical verification on ASIC: KECCAK- $f$ [400]

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